Abstract: The emergence and development of two-dimensional (2D) materials has provided a new direction for enhancing the thermoelectric (TE) performance due to their unique structural, physical and chemical properties. However, the TE performance measurement of 2D materials is a long-standing challenge owing to the experimental difficulties of precise control in samples and high demand in apparatus. Until now, there is no universal methodology for measuring the dimensionless TE figure of merit (ZT) (the core parameter for evaluating TE performance) of 2D materials systematically in experiments. Raman spectroscopy, with its rapid and nondestructive properties for probing samples, is undoubtedly a powerful tool for characterizing 2D materials as it is known as a spectroscopic 'Swiss-Army Knife'. Raman spectroscopy can be employed to measure the thermal conductivity of 2D materials and expected to be a systematic method in evaluating TE performance, boosting the development of thermoelectricity. In this review, thermoelectricity, 2D materials, and Raman techniques, as well as thermal conductivity measurements of 2D materials by Raman spectroscopy are introduced. The prospects of obtaining ZT and testing the TE performance of 2D materials by Raman spectroscopy in the future are also discussed.

Keywords: Raman spectroscopy; two-dimensional materials; thermoelectricity; thermal conductivity; graphene

1. Introduction

Thermoelectricity, which is a property of materials of directly realizing the transformation between heat and electric energy, has attracted extensive research interest due to the issues of severe energy wastage and insufficient resources affecting society. Since the Seebeck effect was discovered in 1821, the development of thermoelectricity is contingent on seeking and discovering new thermoelectric (TE) materials with a high figure of merit (ZT) [1–4]. It is imperative to identify novel TE materials or to develop the new methods to promote TE performance of known materials, realizing their wide applications in industry. In 2004, Novoselov and Geim successfully prepared single-layer graphene by a mechanical exfoliation method [5], which greatly stimulated studies on two-dimensional (2D) materials. Subsequently, layered molybdenum disulfide (MoS2), hexagonal boron nitride (h-BN), black phosphorus (BP), etc. were investigated, expanding the 2D materials family and promoting their development in electronics, photonics, mechanics, and thermotics [6–12]. Importantly, owing to their
unique properties, 2D materials have attracted tremendous attention to thermoelectricity and become potential candidates for advancing TE performance [13–20]. However, it is difficult to exactly measure the TE performance of 2D materials due to their unique structure properties and a new measurement system applied for 2D materials is needed.

Based on the discovery of the light scattering effect in 1928, Raman spectroscopy has become a versatile tool to characterize materials. Raman spectroscopy can provide both structural and electronic information of samples rapidly and non-destructively, being one of the most important techniques for studying 2D materials [21]. The thermal conductivity of materials is a critical parameter to evaluate the TE performance, whereas its measurement in 2D materials is a difficult task. Balandin et al. firstly employed Raman spectroscopy to measure the thermal conductivity of suspended single-layer graphene in 2008 [22], leading to a fruitful advancement in the experimental thermal studies of 2D materials. This method provides the possibility for systematic testing of TE properties, and is guiding the significance for the development of TE materials in the future. This review starts by introducing the background and advancement of thermoelectricity, briefly presenting the development of 2D TE materials. This method provides the possibility for systematic testing of TE properties, and is guiding the significance for the development of TE materials in the future. Then, we review the working principles and applications of Raman spectroscopy. Finally, several examples of how Raman spectroscopy can be used to measure the thermal conductivity of 2D materials are discussed in detail. Prospects, ideas and challenges for the comprehensive measurement of 2D TE performance in the future are reviewed as well.

2. Thermoelectric and 2D Materials

2.1. Background of Thermoelectricity

The TE effect comprises the Seebeck and the Peltier effects. In 1821, Seebeck found that the magnetic needle deflected in the presence of different connected metals under a temperature gradient. Essentially, the electric current was generated by different conductors under a temperature difference, and a magnetic field was generated by the current relying on the Oersted electromagnetism effect, which effected the deflection of the magnetic needle.

![Figure 1. Illustration of TE effect and represented devices. (a) Schematic of the Seebeck effect. Electric current is produced when P-type and N-type semiconductors are placed under temperature differences at the same time. (b) Schematic of the Peltier effect. Heating or cooling is generated when electric current flows through P-type and N-type semiconductors. (c) Schematic of a TE generator. To improve the system-level conversion efficiency, P-type and N-type semiconductor pellets are connected in parallel under ceramic substrates, forming TE devices. Reproduced with permission from [2]. Copyright 2008, American Association for the Advancement of Science.](image-url)
The phenomenon of generating electricity by employing a temperature difference is thus called the Seebeck effect. As shown in Figure 1a, if the N- and P-type semiconductors module at the top is the heat input and at the bottom is the heat removal part, carriers in semiconductors driven by the temperature difference move from the heat terminal to the cool terminal, producing an electron flow from the P-type semiconductor to the N-type semiconductor in the TE module. This is based on the Seebeck effect. The Peltier effect, observed by Peltier in 1834, is the inverse of the Seebeck effect. As shown in Figure 1b, heating or cooling is generated when a TE module is under a voltage, due to carriers taking away heat while moving under the electric field. Besides, the Thomson effect also exists, but can be neglected in this system. Thus, the TE effect mainly consists of the Seebeck and Peltier effects, which are the basis of TE devices. Figure 1c is the illustration of TE devices types, which are connected by large numbers of N- and P-type semiconductors modules in series to increase operating voltage and spread heat flow [2,3].

TE materials have extensive applications, mostly related to TE power generation and refrigeration technology. The former includes waste heat recovery, use of solar energy, and power supplying for wearable electronics [23–26]. The latter is widely applied in many areas of electric refrigeration due to its solid-state nature, absence of vibrations, simplicity and environmental friendliness [27].

The criteria of evaluating TE materials performance is the conversion efficiency between heat and electricity, which is directly related to the dimensionless TE figure of merit ($ZT$). For a generator, their relationship could be expressed as [1]:

$$\eta = \frac{T_h - T_c}{T_h} \cdot \frac{\sqrt{1 + ZT} - 1}{\sqrt{1 + ZT} + \frac{T_c}{T_h}} \quad (1)$$

where $\eta$ is conversion efficiency, $T_h$ and $T_c$ are the temperature of heat and cool terminals, respectively.

As it is shown, the generator efficiency depends on $ZT$ strongly, thus optimizing $ZT$ is a primary operation for enhancing TE performance. Before introducing the $ZT$ value, Seebeck coefficient needs to be a simple explanation. The Seebeck coefficient is a parameter in Seebeck effect, which is a measure of the TE voltage generated per degree of temperature difference between two terminals of the semiconductor module. The definition is given below:

$$S = \frac{dV}{dT} \quad (2)$$

where $S$ is Seebeck coefficient, $V$ is the TE voltage. $ZT$ is defined as

$$ZT = S^2\sigma T / \kappa \quad (3)$$

in which $\kappa$ represents thermal conductivity and $\sigma$ represents electrical conductivity. From this formula, it is obvious that $ZT$ depends on the Seebeck coefficient, absolute temperature $T$, the electrical conductivity, and the thermal conductivity. However, $S$, $\sigma$, and $\kappa$ are interrelated in traditional bulk TE materials, so it is very difficult to control these variables independently to enhance $ZT$. The interdependencies are mainly reflected in two aspects. One is between the Seebeck coefficient and the electrical conductivity in specific materials. For metals or degenerate semiconductors (parabolic band, energy-independent scattering approximation) the $S$ is given by:

$$S = \frac{8\pi^2 k_B^2}{3e \hbar^2} m^* T \left( \frac{\pi}{3n} \right)^{\frac{1}{2}} \quad (4)$$

and $\sigma$ is expressed as:

$$\sigma = ne\mu \quad (5)$$

where $k_B$ is Boltzmann constant, $m^*$ is the effective mass of the carrier, $n$ is the carrier concentration, and $\mu$ is the carrier mobility. To ensure that the Seebeck coefficient is large at certain temperature, one way
is to raise the effective mass, and the other is to reduce the carrier concentration. However, both are impracticable because both can reduce the electrical conductivity according to Equation (5). The other interdependency stems from the electrical conductivity and the thermal conductivity. The thermal conductivity mainly consists of two parts, which are $\kappa_e$ coming from electrons or holes transporting heat, and $\kappa_l$ coming from phonons traveling through the lattice, respectively. This can be expressed as:

$$\kappa = \kappa_e + \kappa_l$$  \hspace{1cm} (6)

According to Wiedemann–Franz law, the electrons’ thermal conductivity ($\kappa_e$) is directly related to the electrical conductivity ($\sigma$):

$$\kappa_e = L\sigma T$$  \hspace{1cm} (7)

where $L$ is the Lorenz factor that is a constant varying with carrier concentration. These clearly show enhancement on $ZT$ is a tricky thing due to the coupled relationship of the thermal and the electrical conductivities [1].

The correlation and complexity between the parameters which are ubiquitous in conventional TE materials, increasing the difficulties of optimizing $ZT$ and being the major causes limiting the development of thermoelectricity.

2.2. Development of TE Materials

Under the efforts of many scientific researchers around the world, the development of traditional bulk TE materials has made great progress [28–30]. Bismuth telluride (Bi$_2$Te$_3$) and its alloys are the classical TE materials with large Seebeck coefficients and are widely used in the commercial field [31–34]. Silicon germanium (SiGe) and its alloys are excellent TE materials suitable for high temperature applications, that are used in TE modules for deep-space missions to convert radio-isotope heat into electricity [35,36]. Lead telluride (PbTe) is also a perfect TE material studied by researchers all the time [37,38]. In addition, skutterudite [39,40], half-Heusler [41], clathrates [42], etc. also cause great interest and have become an indispensable part of the TE family. Other than these, SnSe was studied in depth by Zhao et al. [43,44] and Wei et al. [45] in recent years, becoming a promising TE material.

It is shown that most state-of-the-art TE materials have maximum $ZT$ values between 1 and 2.5 [46]. Nevertheless, such a value is not enough to achieve large-scale application of thermoelectricity [47]. It is necessary to promote the TE property of materials, in which one intriguing way is to explore low-dimensional materials. The two interdependencies of parameters influencing $ZT$ discussed above, in a way, can be decoupled in low-dimensional materials. The reasons can be explained as: (1) enhancing the Seebeck coefficient as well as controlling the Seebeck coefficient and electrical conductivity independently because of quantum-confinement effects, (2) increasing the ratio of electrical conductivity to thermal conductivity taking advantage of numerous interfaces to scatter phonons more effectively than electrons. Both theoretical studies and experimental results show that reducing the material dimensions can increase the $ZT$ value of TE materials [48–51]. Low-dimensional materials are pointed out to provide a new direction on designing high-performance TE materials [33,52–56]. Low-dimensional materials include zero-dimensional (0D), such as quantum dots; one-dimensional (1D) ones, such as nanowires; and 2D materials, such as quantum wells and superlattices. This review mainly involves 2D materials.

2.3. 2D Materials

2D materials are crystalline materials consisting of single or a few layers of atoms with the lateral size being much larger than the thickness. The main categories of 2D materials are shown in Figure 2, which can help grasp and understand the 2D materials in a macroscopic way. Since the successful preparation of graphene, the employment of 2D materials has become a possibility, triggering a boom in the study of 2D materials. The continuous improvement of 2D material preparation technology [7] and manipulation of materials at the atomic scale [57,58], have greatly promoted the development
of 2D materials and 2D devices [59–62]. 2D materials are widely applied in nanoelectronics and optoelectronics due to their outstanding optical, electronic, and other physical properties [63]. The multiplicity of the types and properties of 2D materials provide a broad space for the development of thermoelectricity. The two-dimensionalization of materials, for one thing depending on increasing the density of states near $E_F$ (Fermi level) to enhance the Seebeck coefficient, for another using the interface scattering of phonons to reduce the thermal conductivity, is advantageous for the improvement of TE performance. In recent years, graphene [64,65], transition metal dichalcogenides (TMDs) [66–70], MXenes [15,71,72], etc. were found to possess excellent TE performance, paving the way for further exploration of 2D TE materials.

Figure 2. Schematic of 2D layered materials with their names. (Graphene) Reproduced with permission from [73]. Copyright 2014, American Chemical Society. (TMDs) Reproduced with permission from [74]. Copyright 2011, Nature Publishing Group. (h-BN) Reproduced with permission from [75]. Copyright 2016, Multidisciplinary Digital Publishing Institute (MDPI). (MXenes) Reproduced with permission from [76]. Copyright 2015, American Chemical Society. (BP) Reproduced with permission from [77]. Copyright 2014, Nature Publishing Group. (Others) Reproduced with permission from [78]. American Association for the Advancement of Science.
2.4. Advancement of 2D TE Materials

Advancement of 2D TE materials is the most representative example in term of the strategy of reducing the dimensionality to increase ZT. Thin-film materials as a class of 2D materials, are widely studied for their excellent TE performance and have made great progress in enhancing TE performance. In 2001, Venkatasubramanian et al. first reported on a Bi$_2$Te$_3$/Sb$_2$Te$_3$ superlattice film material prepared by metal organic chemical vapor deposition, which increases the ZT up to 2.4 [79]. Subsequently, Harman et al. used a molecular beam epitaxy technique to prepare a PbSe$_{0.98}$Te$_{0.02}$/PbTe quantum dot superlattice film with a ZT of 2.0 or higher at 300 K in 2002 [80]. Until now, superlattice films remain one of the most attractive research directions in the field of thermoelectrics. In 2017, Tian et al. presented an exfoliation-and-reassembly approach to produce a flexible N-type TiS$_2$/organic superlattice film for low-temperature TE applications, which shows a high power factor ($S^2\sigma$) after annealing under vacuum [81]. Al$_2$O$_3$/ZnO superlattice film [82] and V-telluride superlattice thin films [83] were reported in succession, and they show promising TE performance.

Besides superlattice films, the development of layered 2D TE materials is also endless. Sharma et al. studied the TE properties of 2D telluride (Te) by first principles calculations and semiclassical Boltzmann transport theory, and the maximum ZT = 0.8 was achieved [13]. Monolayer PdSe$_2$ was investigated by Qin et al. and its ZT reached 1.1 along the x direction for P-type doping at room temperature [84]. The TE properties of 2D InSe, SnSe, Pb$_2$Se$_3$, MoS$_2$, and GeAs$_2$ were also studied through theoretical and experimental studies in recent years [14,20,67,85–88]. As it is shown in Figure 3a, the development of TE materials has been rapid in recent years. In the theoretical category, ZT has reached and exceeded 2.5, and 2D materials such as SnSe, Cu$_2$S and BiCuSeO have contributed greatly.

![Figure 3](image-url)  
Figure 3. TE figure of merit (ZT) of materials. (a) Representation of the maximum ZT values of various 2D and traditional TE materials. Among them, SnSe [87], Cu$_2$S [89], Cu$_2$Se [90], and BiCuSeO [91] are investigated to have 2D or quasi-2D characteristics. Reproduced with permission from [46]. Copyright 2017, American Association for the Advancement of Science. (b) Comparison histogram of ZT values for diverse configuration of MoS$_2$, WS$_2$, MoSe$_2$, and WSe$_2$ studied by theoretical calculation. Here (10,0) and (6,6) are from the nomenclature representing armchair and zigzag single-wall Transition metal dichalcogenide nanotube (TMDNT). The different colors of columns refer to the extent of ZT value. From this histogram, one can see monolayer TMDs have a perfect ZT value clearly. Reproduced with permission from [67]. Copyright 2015, American Chemical Society.
2D materials. (1) The interdependencies among the parameters of $ZT$ in 2D materials can be decoupled to a certain degree discussed above, which is beneficial to optimize the $ZT$ by decreasing the thermal conductivity due to phonon interface scattering. 2D TE materials have great room for improvement. (2) 2D materials are excellent for studying flexible, stretchable, and skin-friendly devices, which in conjunction with thermoelectricity, will facilitate the development of, for example, self-powered devices and TE sensors. (3) 2D TE materials enable the fabrication and application of miniaturized and integrated devices. It is worth mentioning that, the chip heat dissipation problem has become a major factor in limiting the development of integrated circuits (IC). 2D TE materials are able to be integrated into IC chips and take advantage of the waste heat supplying electricity for IC, accelerating the advancement of IC industry. All of the above signs indicate that the 2D TE materials are competitive candidates in the field of future thermoelectricity.

The $ZT$ parameter for evaluating the performance of TE materials is conventionally obtained by measuring the thermal and electrical conductivities, the Seebeck coefficient of the TE material at a certain temperature. The measurement of the $ZT$ in the bulk materials is relatively facile. Nevertheless, the test method of $ZT$ for the film and the superlattice TE materials has higher requirements in terms of technology and sample preparation. Thus, a specially designed technique is required urgently. However, so far, a universal standard of systematically measuring $ZT$ of 2D materials is still lacking owing to the experimental difficulties of precise control in samples and high demands on the apparatus. In 2018, Wang et al. summarized the instruments for measuring the Seebeck coefficient of thin-film thermoelectric materials [92]. For measuring thermal conductivity of 2D materials, the Raman spectroscopy technique is an effective method due to its non-destructive properties and simple operation. Besides, the time-domain thermoreflectance (TDTR) technique has also become a popular method in measuring thermal conductivity of films and micro-sized materials in recent years. They all have their own challenges and advantages. For instance, TDTR is an attractive approach to measuring the challenging interface thermal conductivity of dissimilar materials, and has an ultrafast measurement speed. Nevertheless, it has been challenging to measure thermal conductivity along different directions and its measurement process is relatively complex [93,94]. In contrast, the Raman method of measurement is much simpler.

3. Raman Technique

3.1. The Principles of Raman Spectroscopy

Raman spectroscopy is a technique used to identify molecules, study chemical bonding, characterize microstructures of materials, measure thermal conductivity, etc. by measuring the frequency shift of inelastic scattered light from the sample based on their unique vibrational characteristics (fingerprints). The Raman scattering effect was predicted first theoretically by Smekal in 1923 and discovered by C.V. Raman in an experiment in 1928 [95], which is the basis of Raman spectroscopy. In the 1960s, a single-wavelength sources became possible owing to the advent of lasers, which promoted the experimental applications of Raman spectroscopy. Figure 4a illustrates the principle of elastic (Rayleigh) and inelastic scattering. When an incident light ray focuses on the sample through the microscope objective at a defined magnification, Rayleigh scattering, fluorescence, anti-Stokes and Stokes Raman scattering are produced [96]. Among them, fluorescence is harmful to Raman spectroscopy, and is usually suppressed. Anti-Stokes and Stokes Raman scattering is collected by a detector and their diagrammatic sketch is presented in Figure 4b. When an incident lightbeam focuses on the samples, photons interact with chemical bonds or electronic clouds and produce an oscillating polarization in the molecules, exciting the electrons to the virtual energy levels. As it is shown in Figure 4b, electrons on virtual energy levels transfer to the original energy level and emit photons due to the instability of electrons on virtual energy levels, which process is called Rayleigh scattering. There is no energy change in Rayleigh scattering. Rayleigh scattering does not carry related information about sample molecules, which is different from Raman scattering. Anti-Stokes and
Stokes Raman scattering is inelastic scattering, in which the transition energy of electrons excited by incident photons are different from the energy of emitted photons of light. In Stokes Raman scattering, the frequency of the incident photons is higher than the emitted photons, meaning that the incident photons have a higher energy than emitted photons, while in anti-Stokes scattering, the incident photons are of lower energy than emitted photons. Besides, the intensity of anti-Stokes scattering is weaker than Stokes scattering, so Stokes scattering is more remarkable in experiments. Figure 4c shows a typical setup of the confocal micro-Raman spectroscopic system. The sample to be tested is placed on the sample stage, and the information of Raman scattering (mainly Stokes scattering) produced by the system is gathered by the final detector [97].

Through subsequent analysis using a computer system, the Raman spectrum with the appearance as shown in Figure 4e is obtained. Figure 4d illustrates the optical vibration modes of TMDs, which can be characterized by Raman spectroscopy. Different vibration modes store different molecules information, which can be reflected in Raman spectra. $A_{1g}$ and $E_{2g}$ are two typical vibration modes in TMDs. The positions of Raman shift of $A_{1g}$ peak or $E_{2g}$ peak are analyzed and used to clearly distinguish single and few layered TMDs as shown in Figure 4e.
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... process is called Rayleigh scattering. There is no energy change in Rayleigh scattering. Rayleigh scattering does not carry related information about sample molecules, which is different from Raman scattering. Anti-Stokes and Stokes Raman scattering is inelastic scattering, in which the transition energy of electrons excited by incident photons are different from the energy of emitted photons of light. In Stokes Raman scattering, the frequency of the incident photons is higher than the emitted photons, meaning that the incident photon has more energy, while in anti-Stokes scattering, the incident photon is of lower energy. Besides, the intensity of anti-Stokes scattering is weaker than Stokes scattering, so Stokes scattering is more remarkable in experiments.

Figure 4(c) shows a typical setup of the confocal micro-Raman spectroscopic system. The sample to be tested is placed on the sample stage, and the information of Raman scattering (mainly Stokes scattering) produced by the system is gathered by the final detector.

3.2. Application of Raman Spectroscopy

Raman spectroscopy is a non-invasive and non-destructive technique, which requires almost no sample treatment, being suitable for solid state, aqueous conditions and gas phase, as well as film samples. Thus, the applications of Raman spectroscopy are greatly expanded. At present, Raman spectroscopy has a wide range of applications in the fields of chemistry, biomedicine, physics, and so on [100–102]. Raman spectroscopy is also made great contributions to the study of TE materials [103]. With the increasing technical requirements, Raman spectroscopy has now developed into multiple branches, e.g., resonance Raman spectroscopy, surface enhanced Raman spectroscopy [104,105], tip enhanced Raman spectroscopy [106], and micro Raman spectroscopy etc. Micro-Raman spectroscopy
is one of the most important techniques to characterize nanomaterials, which can identify the number of layers of film materials [107], analyze the vibration modes of 2D materials in diverse case [71], and measure the thermal conductivity [22,108–110].

3.3. Raman Spectroscopy for Measuring Thermal Conductivity of 2D Materials

As one of the main parameters for characterizing TE performance, the thermal conductivity has been measured by employing Raman spectroscopy on some layered materials. The following sections discuss graphene, h-BN, BP, and TMDs in details.

3.3.1. Graphene

Graphene is a single layer of carbon atoms bonded through $sp^2$ hybridization with regular hexagonal honeycomb crystal structure exfoliated from graphite. The model diagram of graphene is shown in Figure 2. Graphene has attracted tremendous attention since its successful preparation, owing to its excellent optical [111], electrical [5], mechanical [112], and thermal properties [22,113]. Recently, graphene has also triggered great interest as a new type of TE material and led to a prosperous development [64,114–116]. However, its application in thermo-electrics is limited by the high thermal conductivity and the low Seebeck coefficient due to its gapless spectrum. Hence a series of methods for optimizing TE performance of graphene by enhancing its Seebeck coefficient or decreasing the thermal conductivity have emerged, including modification of graphene band structure, nanostructures [115,117], doping, and graphene-based polymer nanocomposites and so on [118,119]. That makes graphene a promising TE material and promotes its applications [120], such as TE cooling [121].

Raman spectroscopy as a versatile tool, provides a novel method in measuring the thermal conductivity and promotes the development of graphene on thermoelectricity in experiment. Before 2008, although a large number of theoretical studies showed that graphene has a high thermal conductivity [122,123], which has not been confirmed experimentally due to the lack of conventional methods for measuring 2D materials.

Balandin et al. developed noncontact micro-Raman spectroscopy to measure the thermal conductivity of graphene according to the temperature dependence of the frequency of G peak in the Raman spectra [22,124–128]. The schematic setup of the experimental device is shown in Figure 5a and details are shown in Figure 5b,c for clarity. The focused laser light exposes on the middle of suspended single-layer graphene (SLG), forming a hot spot and diffusing around by heat waves, which produces a stable temperature gradient on the graphene. At the same time, the laser is also acted as an incident source for Raman spectroscopy, and the Raman spectrum of SLG is gained by analyzing Raman scattering light, which is shown in Figure 5d. The position of G and 2D peaks are $\sim$1583 cm$^{-1}$ and $\sim$2700 cm$^{-1}$ at room temperature, respectively. When the laser power changes, the position of the peak will also change. Figure 5e is the Raman spectrum of G peak at two different laser powers and shows the weak evolution of Raman shift of G peak. For the graphene suspended on trench shown in Figure 5b, when the laser hot spot is much smaller than the width of the SLG sample, it can be considered that the heat waves move in two opposite directions toward the trench edges, assuming that temperature of the trench edges is consistent with the heat sink and room temperature. Then, the thermal conductivity of the sample can be expressed as:

$$\kappa = \frac{d}{2A} \frac{\Delta P}{\Delta T}$$

where $d$ is the distance from the middle of the suspended SLG to the heat sink with the temperature ambient $T$ and cross-sectional area $A = h \times W$ ($h$ and $W$ is the thickness and width of SLG, respectively). Thus, the thermal conductivity of SLG will be calculated if the laser power absorbed $\Delta P$ by SLG and the resulting local temperature rise $\Delta T$ are measured out. The success of this work is benefited from a previous work on graphene by Calizo et al. This work demonstrated that the frequency of G peak in
the Raman spectra of graphene on Si/SiO$_2$ substrates is dependent on temperature, concluding the relation of:

\[ \omega = \omega_0 + \chi_T T \tag{9} \]

where \( \omega \) and \( \omega_0 \) are the frequencies of the G peak at temperature T and T extrapolated to 0 K, respectively. \( \chi_T \) is temperature coefficient, which defines the slope of the dependence [124]. In this work, \( \chi_T \) was calculated by the fitted straight dash line slope in Figure 5f. Through the processing of relation (8) and (9), the thermal conductivity can be expressed as:

\[ \kappa = \chi_T \cdot \frac{d}{2hW} \cdot \Delta \omega \cdot \frac{1}{\delta T} \tag{10} \]

Figure 5. The group diagram for measuring the thermal conductivity of single graphene by micro-Raman spectroscopy. (a) Schematic of experiment model for measurement. In this schematic, the focused laser light exposure on a graphene layer suspended across a trench producing a hot spot and being incident light of Raman spectroscopy. The heat sink is graphitic layer to ensure good heat dissipation at the edge of the layer of graphene. Reproduced with permission from [22]. Copyright 2008, American Chemical Society. (b) The vertical scanning electron microscopy image of the suspended graphene flakes where one can clearly see the trench and suspended graphene. (c) The front view of experiment model. In this schematic, one can more clearly see that a hot spot generates heat waves inside single-layer graphene (SLG) propagating toward heat sinks. In addition, the silicon substrate and the upper silicon oxide are also given for clarity. Reproduced with permission from [125]. Copyright 2008, American Institute of Physics. (d) Raman spectrum of suspended graphene showing the G peak (at ~1583 cm$^{-1}$) and 2D peak (at ~2700 cm$^{-1}$) at room temperature excited at 488 nm. (e) Raman spectrum of G peak at two different laser power. The red and blue lines represent 0.950 and 2.168 mW, respectively. Weakly evolution of Raman shift of G peak occurs in different laser power. (f) Temperature dependence of the G peak frequency for the single layer graphene. The solid square black spots are experimental data of G peak position at a certain temperature and the fitted straight dash line slope is the temperature coefficient which is $-0.016$ cm$^{-1}$/$^\circ$C Reproduced with permission from [124]. Copyright 2007, American Chemical Society. (g) The G peak position shift dependence of total dissipated laser power excited at 488 nm. The fitted straight dash line slope is the power coefficient. The inserted chart illustrates a method of fitting data using linear regression equations where the values of parameter A and B are given. Reproduced with permission from [22]. Copyright 2008, American Chemical Society.
The above equation involves the changes of $G$ peak frequency with laser power absorbed by SLG—$\delta \omega / \delta P$, which is the only unknown factor in the equation at present. Figure 5g is the $G$ peak position shift dependence of total dissipated laser power, in which the fitted straight dash line slope is $\delta \omega / \delta P_D$ (or $\chi_P$), where $P_D$ is the total laser power, and $P_D = P + P_{Si}$, where $P_{Si}$ is laser power absorbed by Si. The amount of the power $P$ absorbed by the suspended graphene can be evaluated through the calibration procedure with pyrolytic graphite (for detailed steps, see [22]). Thus, through the above process, the thermal conductivity about $5300 \pm 480 \text{ Wm}^{-1}\text{K}^{-1}$ of graphene at room temperature is obtained, which was the first time the challenge of measurement on thermal conductivity of graphene experimentally was overcome [22].

In addition, Chen et al. used micro-Raman spectroscopy to measure the thermal conductivity of monolayer graphene of variable sizes in vacuum and gaseous environments in 2011, which values range from $(2600 \pm 900)$ to $(3100 \pm 1000) \text{ Wm}^{-1}\text{K}^{-1}$ near $350 \text{ K}$ [129]. Lee et al. also measured the thermal conductivity in suspended pristine graphene by Raman spectroscopy in 2011, which values range from $\sim 1800 \text{ Wm}^{-1}\text{K}^{-1}$ near $325 \text{ K}$ to $\sim 710 \text{ Wm}^{-1}\text{K}^{-1}$ at $500 \text{ K}$ [130]. These successes of experiments on measuring thermal conductivity by Raman spectroscopy pave a new way to measure TE performance of 2D TE materials, and are vital to the advancement of 2D thermoelectricity.

3.3.2. h-BN

Boron nitride (BN), which exists in Nature, consists of equal numbers of boron (B) and nitrogen (N) atoms [131]. h-BN is one form of the BN, which is the most stable BN phase under ambient conditions [132]. An atomic model of h-BN is shown in Figure 2. As it is shown, h-BN is one kind of 2D materials, which has a layered crystal structure with alternating B and N atoms. It is also called “white graphene” as a single-layer h-BN nanosheet can be regarded as a graphene analogue [7]. Similar structures often lead to some common features, such as high mechanical strength and thermal conductivity, as well as good lubrication [132]. There are also many properties distinct from graphene in h-BN, and it is significant to explore these dissimilarities and employ them in what is not applied in graphene. The most striking difference is that h-BN possesses a huge bandgap while graphene is gapless, so that it can act as an insulating layer or dielectric substrate [133]. h-BN was rarely investigated separately as TE materials due to its intrinsic properties about the low electrical conductivity and the high thermal conductivity.

The thermal conductivity of atomically thin h-BN has been explored [108,110,134–138], experimentally. It can reach to 484 W·m⁻¹·K⁻¹ in bilayer h-BN as measured by suspended prepatterned microstructures [137], and around 360 W·m⁻¹·K⁻¹ in 11-layer h-BN measured by a microbridge device with built-in thermometers [138] at room temperature. Zhou et al. reported an experiment that used noncontact micro-Raman spectroscopy as another excellent method to measure thermal conductivity of layered h-BN in 2014 [108]. Raman spectroscopy plays an important role in evaluating the thermal conductivity of thin h-BN sheets. Figure 6a shows the schematic of an experimental setup for measuring the thermal conductivity of h-BN sheets by micro-Raman spectroscopy. A 514.5 nm laser excited with a ~1 µm spot size is focused on the middle of suspended layered h-BN under ambient conditions, depending on golden heat sink to dissipate heat and maintain a stable temperature gradient. For evaluating the thermal conductivity, there are two parameters that should be measured by this setup according to Equation (10). The first is the first-order temperature coefficient $\chi_T$ in the Raman scattering. On the basis of the results described in [108], the Raman $E_{2g}$ mode red-shifts of layered h-BN are sensitive to surrounding temperature, in that Raman $E_{2g}$ mode peak shifts 4.0 cm⁻¹ with the temperature increasing from 313 to 433 K as it shown in Figure 6b. The temperature-dependent peak frequency of $E_{2g}$ mode of single-layer h-BN is shown in Figure 6c, and from the fitted line, first-order temperature coefficient $\chi_T$ is obtained. The other parameter for the thermal conductivity measurement of h-BN is the dependence of the Raman $E_{2g}$ mode frequency on the laser power $\delta \omega / \delta P$ ($\chi_P$). Figure 6d is the image of $E_{2g}$ mode peak frequency as a function of the laser power, and the $\delta \omega / \delta P$ can be extracted from the slope of fitted line. Then, based on acquiring the ratio of laser power
absorbed by h-BN, the thermal conductivity can be calculated in the range from 227 to 280 W·m⁻¹·K⁻¹ at room temperature.

3.3.2 h-BN

Boron nitride (BN), which exists in Nature, consists of equal numbers of boron (B) and nitrogen (N) atoms [131]. h-BN is one form of the BN, which is the most stable BN phase under ambient conditions [132]. An atomic model of h-BN is shown in Figure 2. As it is shown, h-BN is one kind of 2D materials, which has a layered crystal structure with alternating B and N atoms. It is also called “white graphene” as a single-layer h-BN nanosheet can be regarded as a graphene analogue [7]. Similar structures often lead to some common features, such as high mechanical strength and thermal conductivity, as well as good lubrication [132]. There are also many properties distinct from graphene in h-BN, and it is significant to explore these dissimilarities and employ them in what is not applied in graphene. The most striking difference is that h-BN possesses a huge bandgap while graphene is gapless, so that it can act as an insulating layer or dielectric substrate [133]. h-BN was rarely investigated separately as TE materials due to its intrinsic properties about the low electrical conductivity and the high thermal conductivity.

3.3.3. BP

BP is an emerging 2D material with potential applications in electronics and optoelectronics [139–145]. BP is a layered material as shown in Figure 2, in which individual layers stack together through the van der Waals force, much like bulk graphite, and was also successfully prepared by mechanical exfoliation. Monolayer BP is composed of a puckered honeycomb structure, in which one P atom bonds with the other three. The structure of BP is anisotropic with the zigzag and the armchair directions marked in Figure 7a, which results in its anisotropic transport properties [7,136,146–148]. Importantly, the bandgap of BP is tunable depending on its thickness, and is highly sensitive to the plane strain and edge structures on prediction [149,150]. Both the intrinsic in-plane anisotropy and the moderate bandgap of BP also promote considerable development of TE application [151–157]. In addition, BP is theoretically predicted to be a promising TE material [154,155,158–160] due to its high carrier mobility [161], large Seebeck coefficient, as well as relatively low thermal conductivity [109,162], and the experimental research on thermoelectricity of BP is also in full swing [163].
However, it is apparent that the experimental research is much less than the theoretical prediction on thermoelectricity of BP, because experimental measurements are much more complex and difficult. Raman spectroscopy is a very powerful tool to characterize flakes, and using this technique, previous studies reported the identification of thicknesses for BP [164]. The present status of Raman spectroscopy in BP are concluded by Ribeiro et al. [165]. More importantly, Raman spectroscopy is also a perfect method in measuring thermal conductivity of layered BP [109,162,166], which will lead to a prosperous advancement in thermoelectricity of BP.

![Figure 7](image_url)

**Figure 7.** Structure characterization of BP and the process on its thermal conductivity measurements using micro-Raman technique. (a) Diagram of the lattice structure of BP. Directions of zigzag and armchair are indicated. (b) Atomic vibrational patterns of A_g1, B_2g and A_g2 phonon modes from the front view. (c) Raman spectra of BP at different directions and vibrational patterns. ‘VV’ and ‘VH’ are two configurations standing for different directions of laser polarization to gain the A_g and B_2g vibrational patterns. Zigzag is represented by red lines and armchair is represented by blue lines. (d) Illustration of experiment model for measuring suspended BP flakes. Here He-Ne laser through aperture and collecting mirror exposures on the suspended BP laying SiN substrate. (e) The Raman spectra of BP flakes at 72, 57, 42 and 24 °C. The three modes of vibration patterns are marked with dashed lines in the diagram so that the Raman shift of them are clearly visible. (f) The A_g2 Raman shift as a function of temperature under armchair- and zigzag-polarized laser. The fitted straight dash line slopes are the temperature coefficients. (g) The temperature rise as a function of absorbed laser power of BP film along armchair and zigzag directions. Reproduced with permission from [109]. Copyright 2015, Nature Publishing Group.

The measurement of suspended layered 2D materials by micro-Raman spectroscopy was presented in graphene and h-BN above, whereas BP possesses anisotropic properties and need to distinguish the zigzag and armchair axes using polarized Raman spectroscopy firstly, which was also used by Wu et al. [167] and Ribeiro et al. [168] in 2015 on BP. Figure 7b is the diagram of Raman vibration modes of BP, including in-plane A_g1 and A_g2 mode, as well as the out-of-plane B_2g mode in front view. The different directions show different intensity ratios of A_g2 to A_g1, where the A_g2/A_g1 becomes larger (~2) with armchair-polarized laser excitation and smaller (~1) with zigzag-polarized laser excitation as shown in Figure 7c, which serves as Raman signatures of armchair and zigzag lattice axes and is a basis of studying the anisotropic thermal conductivity of BP. Figure 7d is the illustration of the experimental setup of micro-Raman spectroscopy. By collecting and analyzing the Raman scattering light of the sample, the changes of Raman shift with laser power can be figured out.
In addition, the Raman spectra of BP at different temperature are shown in Figure 7e, from which we can fit straight lines of the Ag\textsuperscript{2} mode in zigzag and armchair axes as shown in Figure 7f. A series of Raman spectra can be obtained under various incident laser power settings, which give the laser power coefficient. In addition to the previously obtained temperature coefficient, the laser-power-dependent temperature rise of BP film is acquired as shown in Figure 7g, which can be expressed as \( \delta T/\delta P_A \). Then, through auxiliary calculations, the thermal conductivity of layered BP is evaluated eventually, which is about 10–20 W·m\textsuperscript{-1}·K\textsuperscript{-1} for thin-film BP [109].

3.3.4. TMDs

TMDs, which are semiconductors of the type MX\textsubscript{2} (M = W, Mo; X = S, Se, Te), are a burgeoning class of 2D materials with novel physical properties and are expected to become an alternative to graphene. TMDs are also layered materials with van der Waals interactions between layers, and a diagram of their structure is shown in Figure 2. Note that TMDs exist in several structural phases owing to different coordination spheres of the transition metal atoms, including trigonal prismatic (2H), distorted octahedral (1T) and dimerized (1T\textsuperscript{′}) phases. TMDs show excellent properties in electronics, optoelectronics, mechanics, chemistry and thermoelectricity, which will enable TMDs to have great potential in the future of technology [169–175]. It is interesting to understand the excellent TE properties of TMDs, which will promote the advancement of thermoelectricity. In recent years, there have been lots of theoretical studies on the TE properties of TMDs by first-principles and density functional calculations, as well as semiclassical Boltzmann transport theory, predicting that TMDs have a competitive TE performance, due to their adjustable electronic properties and high electrical conductivity confined in their 2D planes [16,66,69,70,175–178]. The low thermal conductivity of TMDs is also a critical factor resulting in excellent TE performance, which is from 0.05 to 62.2 W·m\textsuperscript{-1}·K\textsuperscript{-1} in different experiments reviewed by Wang et al. in 2017 [136]. In these experiments, Raman spectroscopy acts a pivotal part in the measurement, especially in MoS\textsubscript{2} and WS\textsubscript{2}. The following emphasizes on the measurement of MoS\textsubscript{2} by Raman spectroscopy.

MoS\textsubscript{2} is one of the most stable layered TMDs, and it has achieved remarkable results in terms of electronic, optoelectronic devices [169,179,180], as well as thermoelectricity [88,181]. Previous works provided a detailed process on measuring thermal conductivity of suspended layered MoS\textsubscript{2} by micro-Raman spectroscopy [110,182–184]. Figure 8a is the schematic of the experiment setup and Figure 8b is the sectional view of 8(a) for clarity. In this experiment, due to the low thermal conductivity of MoS\textsubscript{2}, there is a porous Si\textsubscript{3}N\textsubscript{4} plate with the holes 1.2 \( \mu \)m suspended on SiO\textsubscript{2}/Si substrate, and the MoS\textsubscript{2} sheet was placed thereon, as shown in Figure 8b. At different temperature, the atomic vibrational modes of MoS\textsubscript{2} changes, which contribute to Raman spectra offset as shown in Figure 8c. According to the offset, Figure 8d gives the temperature dependence of Raman peak frequencies from 100 to 320 K for the A\textsubscript{1g} and E\textsubscript{2g}\textsuperscript{1} modes. By the fitted slopes, the temperature coefficient can be calculated. Then, from the offset of Raman spectra of the two modes at different laser power shown in Figure 8e, the Raman peak frequencies as a function of laser power are obtained, which show in Figure 8f. By the fitted slopes, the laser power coefficient can be calculated. Finally, the resulting thermal conductivity \( \kappa = (34.5 \pm 4) \) W·m\textsuperscript{-1}·K\textsuperscript{-1} of MoS\textsubscript{2} at room temperature is evaluated on the basis of the temperature coefficient and laser power coefficient.

The Table 1 summarizes the above data.

From the table, one can clearly see that the thermal conductivities of graphene and h-BN are much more than those of BP and MoS\textsubscript{2}. Therefore, the laser power is lower in the experiment of BN and MoS\textsubscript{2} to avoid local overheating and sample damage. The magnitude of the temperature coefficient is same, which may depend on the similarity of the mechanism of temperature influencing the phonon vibration modes. By analyzing the processes of measuring thermal conductivities of graphene, h-BN, BP, and MoS\textsubscript{2} employing Raman spectroscopy, a promising method in evaluating the thermal conductivity of 2D materials is obtained, which paves the way for efficient thermal management in 2D layered materials.
There have been lots of theoretical studies on the TE properties of TMDs by first-principles and density functional calculations, as well as semiclassical Boltzmann transport theory, predicting that the TE properties of TMDs, which will promote the advancement of thermoelectricity. In recent years, Molecules 2019, 24, x 15 of 25

Table 1. Comparison of the thermal conductivity measurement parameters of different layered samples by Raman spectroscopy at room temperature.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Trench Width (Hole Diameter)</th>
<th>$\chi_T$ (cm$^2$K$^{-1}$)</th>
<th>$\chi_P$ (cm$^2$m$^{-1}$W$^{-1}$)</th>
<th>$\kappa$ (W m$^{-1}$K$^{-1}$)</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Graphene</td>
<td>3 μm</td>
<td>$-0.0162 \pm 0.0020$</td>
<td>$-1.29 \pm 0.11$</td>
<td>$5300 \pm 480$</td>
<td>Balandin et al. [22], Calizo et al. [124]</td>
</tr>
<tr>
<td>h-BN</td>
<td>7 μm</td>
<td>$-0.0341 \pm 0.0012$</td>
<td>$-1.13 \pm 0.12$</td>
<td>$227 \pm 280$</td>
<td>Zhou et al. [106]</td>
</tr>
<tr>
<td>BP</td>
<td>*</td>
<td>Armc -0.019–0.024</td>
<td>*</td>
<td>10–20</td>
<td>Luo et al. [109]</td>
</tr>
<tr>
<td>MoS$_2$</td>
<td>1.2 μm</td>
<td>$A_{1g} -0.013 \pm 0.001$</td>
<td>$A_{1g} -10.9 \pm 0.4$</td>
<td>$34.5 \pm 4$</td>
<td>Yan et al. [110]</td>
</tr>
</tbody>
</table>

* The trench width and $\chi_P$ of BP are not provided in Ref. [109].

4. Conclusions and Outlook

In summary, 2D TE materials, which have been explored and studied widely in the past few years, will become a promising direction on optimizing TE performance. Similar to bulk materials, the measurement on TE performance of 2D materials also involves the electrical and thermal conductivities, as well as the Seebeck coefficient of specimen. Raman Spectroscopy is a precise and powerful method in materials characterization, which is known as a spectroscopic ‘Swiss-Army Knife’. The measurement of the thermal conductivity of 2D materials has been achieved by Raman spectroscopy. Based on it, making an electric test on the specimen in the Raman resting environment at a controllable temperature, obtaining the $\Delta V/\Delta T$ and $\Delta V/\Delta I$, which contributes to calculate the Seebeck coefficient and electrical conductivity, respectively. Eventually, the $ZT$ of 2D TE materials will be evaluated by Equation (3).
It is worth mentioning that, measuring $ZT$ by Raman Spectroscopy combined thermal properties with electrical properties in bulk materials was achieved by Chen et al. and Yu et al. in recent years [185,186], which boosts the advancement of TE research. Extending it to the field of 2D materials will further promote the development of thermoelectricity.

Nevertheless, some challenges still remain in the 2D TE materials and the measurement of their performances:

1. Advancement of 2D TE materials. Studies on 2D TE materials are still in their infancy, so the actual TE performances in the experiments or devices are not ideal enough, and the practical applications are still limited. It is necessary to continue to develop 2D TE materials and promote their performance. To note, high pressure applied to materials can strikingly improve TE performance [185–187], which provides a meaningful idea for advancement of 2D TE materials.

2. The measurement of electric properties of 2D materials. It is difficult to accurately measure the electric properties of 2D materials due to the miniaturization of the scales.

The last few years have witnessed the exciting development of TE materials, in which Raman spectroscopy has undoubtedly made a great contribution, especially for 2D TE materials. With unremitting efforts and struggles of researchers, Raman spectroscopy will boost further advancements of TE materials, contributing to resolving the contradiction between energy waste and insufficient resources in the future.

**Author Contributions:** X.W. and Z.D. conceived, designed, wrote and edited the review. X.W., H.X., F.L., C.L., C.W., X.-J.C., Z.-Y.C., J.Z. modified and revised the review. All authors were involved in writing-review & editing of the paper.

**Funding:** This work is supported by the NSFC under grant Nos. 61574060, Projects of Science and Technology Commission of Shanghai Municipality Grant Nos. 15JC1401800 and 14DZ2260800, the Program for Professor of Special Appointment (Eastern Scholar), and Shanghai Rising-Star Program (17QA1401400), and the Fundamental Research Funds for the Central Universities.

**Acknowledgments:** The authors are grateful to the valuable comments from anonymous referees.

**Conflicts of Interest:** The authors declare no conflict of interest.

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