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OPEN Pressure-induced superconductivity in H₂-containing hydride PbH₄(H₂)₂

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High pressure structure, stability, metallization, and superconductivity of $PbH_4(H_2)_2$, a H_2 -containing compound combining one of the heaviest elements with the lightest element, are investigated by the first-principles calculations. The metallic character is found over the whole studied pressure range, although $PbH_4(H_2)_2$ is metastable and easily decompose at low pressure. The decomposition pressure point of 133GPa is predicted above which $PbH_4(H_2)_2$ is stable both thermodynamically and dynamically with the C2/m symmetry. Interestedly, all hydrogen atoms pairwise couple into H₂ quasimolecules and remain this style up to 400GPa in the C2/m structure. At high-pressure, PbH₄(H₂)₂ tends to form the Pb-H₂ alloy. The superconductivity of T_c firstly rising and then falling is observed in the C_2/m PbH₄(H₂)₂. The maximum of T_c is about 107 K at 230 GPa. The softening of intermediatefrequency phonon induced by more inserted H₂ molecules is the main origin of the high T_{c} . The results obtained represent a significant step toward the understanding of the high pressure behavior of metallic hydrogen and hydrogen-rich materials, which is helpful for obtaining the higher T_c.

In recent decades, many scientists have devote to searching for the high-temperature superconducting materials. For the lightest element, hydrogen (H), Ashcroft applied the BCS theory to propose that the metallic hydrogen will be a room-temperature superconductor under high pressure¹. This suggestion has motivated considerable experimental and theoretical activities. However, solid hydrogen remains insulating character at extremely high pressure, at least up to 342 GPa². Due to the extremely high and experiment unreachable pressure, as a alternative, Ashcroft proposed that the hydrogen-rich alloys shall transform into metal under relatively lower pressure due to the chemical precompressions from the comparable weight elements³. Thus, hydrogen-rich group-IV hydrides have been extensively explored, such as CH_4 , SiH_4 , GeH_4 , SnH_4 , and PbH_4 . All of them show up interesting new structures and novel properties under pressure. CH₄ is still an insulator up to the pressure of 520 GPa⁴. Although Eremets et al. experimentally reported the metallization and superconductivity of SiH₄ above $60 \,\text{GPa}^5$, for the controversial result it might be understood as superconductivity of amorphous silicon, silicon hydrides, or platinum hydrides^{6,7}. And theoretical prediction indicates that the stable SiH_4 can behave as metal and exhibit superconductivity above 220 GPa with the superconducting transition temperature (T_c) of about 20K (The Coulomb parameter $\mu^* = 0.1$, the below is same.)⁸. GeH₄ has lower metallization pressure than silane^{9,10}, and the highest T_c reaches to 73 K at 220 GPa¹¹. Furthermore, the metallization pressure of SnH₄ decreases, the highest T_c is close to 83 K at 120 GPa¹².

It is clearly that the metallization pressure of group-IV hydrides decreases with increase of atomic number of heavy element, which is obviously less than that of solid H₂. Unfortunately, the T_c of group-IV hydrides is also greatly decreased. By analyzing the crystal feature, we find that the quasi-molecular H_2

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Figure 1. Calculated enthalpies per PbH₄(H_2)₂ **unit as the function of pressure.** Enthalpy difference versus pressure for competitive structures of PbH₄(H_2)₂, referenced to the *P*-1 phase. The decomposition enthalpies into PbH₄ + 2H₂, PbH₃ + 5/2H₂, PbH₂ + 3H₂, PbH + 7/2H₂, and Pb + 4H₂ were also plotted. The inset exhibits the change of enthalpies induced by ZPE correction, which indicates that the decomposition pressure of the *C*2/*m* structure decreases as 133 GPa.

units exist in the high-pressure structures of GeH₄ and SnH₄. And these H₂ units have been found to contribute significantly to the superconductivity. Then, whether can the T_c be improved by intercalating H₂ into group-IV hydrides? H₂-containing compounds of CH₄-H₂ have been fabricated up to 30 GPa, such as CH₄(H₂)₂, (CH₄)₂H₂, CH₄(H₂)₄, CH₄H₂¹³. But both metallization and superconductivity are still lack. For the SiH₄-H₂ system, the crystal structure, phase diagram, and metallization under pressure of SiH₄(H₂)₂ were extensively explored¹⁴⁻²². The T_c of SiH₄(H₂)₂ is as high as 107 K at 250 GPa²³, which is visibly higher than that of SiH₄. Following the experimental observation²⁴, we have also theoretically investigated the structural, phase transition, metallization, and superconductivity of GeH₄(H₂)₂ under pressure^{25,26}. The predicted T_c of GeH₄(H₂)₂ is close to 100 K at 250 GPa, higher than that of GeH₄. These results inevitably encourage us further to seek for high-temperature superconductors and study the superconductivity in these H₂-containing compounds. However, it is necessary to decrease the work pressure of superconducting. For examples, the decomposition pressures are as high as 248 GPa for SiH₄(H₂)₂ and 220 GPa for GeH₄(H₂)₂, respectively, above which they are stable superconducting materials.

As mentioned above, the combination the lightest H with one of the heaviest Pb seems to be a good way to improve the T_c and decrease the work pressure. Chemically, PbH₄ still remains the most elusive of group-IV tetrahydrides. The pioneering theoretical work of Desclaux and Pyykkö predicted the structure and stability of $PbH_4^{27,28}$. The theoretically predicted tetrahedral structure of an isolated molecule, with an equilibrium Pb-H distance of approximately 1.73 Å, was eventually confirmed by experiments^{29,30}. But, Krivtsun et al.³⁰ observed that the PbH₄ molecules were kinetically unstable and readily decompose to Pb atomic layer and H₂ in approximately 10s. Recently, Zaleski-Ejgierd et al. theoretically investigated the structure and the stability of PbH₄ under high pressure³¹. They found that PbH₄ is stable thermodynamically above 132 GPa, in forms of Imma (132–296 GPa) and Ibam (>296 GPa) space groups. And PbH₄ even keeps the metallic character covering the whole range of pressure³¹. However, the superconductivity is indeterminate, since the dynamic stable phase of PbH_4 has been not discovered from experimental and theoretical aspects yet. By intercalating H_2 units into PbH₄ molecular crystal, e.g. PbH₄(H₂)₂, how about the structure, stability, and superconductivity? It is just the purpose of our study. In this work, we found out the stable phase of $PbH_4(H_2)_2$ thermodynamically and dynamically and investigated its desired superconductivity. The decomposition pressure of 133 GPa is much lower than the metallization pressure of solid hydrogen, which is easily reached in experiments by diamond-anvil techniques. And the H_2-H_2 coupling under high pressure figures out the different superconducting mechanism.

Results

Covering the wide pressure range of 0–400 GPa, variable-cell structure prediction simulations with 1 to 4 PbH₄(H₂)₂ formula units per cell (f.u./cell) were performed. We have calculated the enthalpies of searched structures of PbH₄(H₂)₂ to examine the thermodynamical stability induced by pressure. For several competitive structures of PbH₄(H₂)₂, the enthalpies (relative to the *P*-1 structure) as function of pressure are shown in Fig. 1. It is found that *Pnnm* phase is the most stablest below 40 GPa with the lowest enthalpy value. Starting from 40 GPa up to 135 GPa, PbH₄(H₂)₂ transfers into *P*-1 phase. Upon further compression, the *C*2/*m* becomes to the most stablest phase above 135 GPa. As a result, there are two structural phase transitions existing in the range of 0–400 GPa. Three low-enthalpy structures were obtained, orthorhombic *Pnnm* (4f.u./cell), triclinic *P*-1 (2f.u./cell), and monoclinic *C*2/*m* (2f.u./cell), respectively, as shown in Supplementary Fig. S1 online. The lattice parameters of these three structures at



Figure 2. High-pressure crystal structure of $PbH_4(H_2)_2$. (a) C2/m structure at 200 GPa. Large and small spheres represent Pb and H atoms, respectively. H1-H4 mark four non-equivalent H atoms on the crystallographic sites. (b,c) show the C2/m structure normal to the (001) and (010) plane, respectively.

different pressures are also listed in Table S1 of the supplementary information online. From the crystal configurations at different pressures, PbH_4 tetrahedral molecule does not exist in $PbH_4(H_2)_2$, and all of hydrogen atoms construct the H₂ quasi-molecules separating from Pb atoms.

However, it was reported that the hydrogen-rich materials is easily decomposed^{10,11,15-17,22-25,31,32}. Hence, we must check the stability by mean of estimating the decomposition enthalpy. For PbH₄(H₂)₂, there are five possible decomposition paths as PbH₄(H₂)₂ \rightarrow Pb+4H₂, 2PbH₄(H₂)₂ \rightarrow 2PbH+7H₂, PbH₄(H₂)₂ \rightarrow PbH₂+3H₂, 2PbH₄(H₂)₂ \rightarrow 2PbH₃+5H₂, and PbH₄(H₂)₂ \rightarrow PbH₄+2H₂, respectively. For three system of PbH₃, PbH₂, and PbH, we searched their structures at different pressures. Structural parameters at different pressure regions are presented in Supplementary (Tables S2, S3, and S4) online. With help of the reported structures of *Pmnm*, *P6/mmm*, *Imma* and *Ibam* for PbH₄³¹, *fcc*, *hcp* and *Im* $\overline{3}m$ for Pb³³, *P6*₃*m*, *C*/2*c*, and *Cmca* for H₂³⁴ corresponding stable pressures, the decomposition enthalpies were calculated and plotted in Fig. 1. PbH₄(H₂)₂ is unstable and decomposes into Pb + 4H₂ blow 120 GPa and PbH₄ + 2H₂ in the pressure range of 120–160 GPa. Namely, both *Pnnm* and *P*-1 phases are metastable. PbH₄(H₂)₂ is only stabilized above the pressure of 160 GPa, displaying the symmetry of C2/*m*.

Besides, it has well-known that quantum effects related to hydrogen atoms are very important. The hydrogen zero-point energy (ZPE) has significantly revised the structural stability as in the cases of solid hydrogen³⁴ and hydrogen-rich materials^{9,11}. To judge the effect on stability, we also calculated the ZPEs of PbH₄(H₂)₂, PbH₄, and H₂ in the range of 100–200 GPa using the quasiharmonic approximation³⁵. As the insert shown in Fig.1, the ZPE effect does not change the order of the phase transitions but lowers the decomposition pressure of the C2/*m* structure into ~133 GPa. This decomposition pressure of PbH₄(H₂)₂ is obviously lower than 248 GPa of SiH₄(H₂)₂²³ and 220 GPa of GeH₄(H₂)₂²⁵, which indicates that PbH₄(H₂)₂ will exist in the wider pressure range. For this stability, the subsequent crystal structural, electronic, phonon, and electron-phonon coupling (EPC) calculations are focused on the C2/*m* structure above 133 GPa, and typical results are presented at 200 GPa.

For C_2/m structure, Pb atoms occupy the crystallographic 2a sites and four non-equivalent H atoms sit on the 4i sites under high pressure. All of H atoms pairwise coupling into two types of quasi-molecules as shown in Fig. 2a. The nearest distance between Pb and H atom is about 2Å. In this dense structure, we can not find any plumbane molecules existing, but H₂ quasi-molecules distribute around Pb atoms and are ordering (Fig. 2). This kind of ordered arrangements of H_2 units is clearer at high pressure, while H_2 units tend to be inordering at low pressure^{18,25}. A visible character of Pb and H_2 in layers is observed from (001)-plane (Fig. 2b) or (010)-plane (Fig. 2c). Noticeably, the layered feature is also a common phenomenon in some hydrogen-rich systems. With the increase of pressure, all of the lattice constants of C2/m structure in a, b, and c directions decrease. However, the H-H bond lengths in H₂ quasi-molecules marked as $d_{1_{H-H}}$ (formed by H1 and H2 sites shown in Fig. 2a) and $d_{2_{H-H}}$ (formed by H3 and H4 sites shown in Fig. 2a) firstly increase then decrease as shown in Fig. 3a. There are three kinds of intermolecular distances among H_2 molecules in the C2/m structure, all of them are monotonously decreased with the pressurizing, as shown in Fig. 3b. Reviewing the high-pressure structural character, we find that part hydrogen atoms form H_2 units with the other hydrogen atoms strongly bonding with Si in *Ccca* phase of SiH₄(H₂) $_{2}^{23}$, while all of hydrogen atoms pairwise coupling into H₂ quasi-molecules with the nearest distance of ~1.7 Å between Ge and H in $P2_1/c$ phase of GeH₄(H₂)₂²⁵. As a comparison, with the help of analysis of atomic distances, the intermolecular and intramolecular couplings of H₂ gradually strengthen, while the interaction between H and the heavy atom evidently weakens from $SiH_4(H_2)_2$ to $GeH_4(H_2)_2$ and then to $PbH_4(H_2)_2$.



Figure 3. The H-H bond lengths in H_2 unit and the H_2 - H_2 intermolecular distances. For C2/m structure, two types of H-H bond lengths in H_2 (**a**) and three kinds of distances among H_2 molecules (**b**) change with pressure (133–350 GPa).

At 200 GPa, the lattice parameters of C_2/m structure are a = 7.184 Å, b = 2.807 Å, and c = 2.973 Å, as well as the angle $\beta = 68.1^{\circ}$ (see Supplementary Table S1 online). The $d_{1_{H-H}}$ and $d_{2_{H-H}}$ are 0.78 Å and 0.82 Å, respectively. The intermolecular distance of H₂-H₂ is less than that between Pb and H atoms. With the lattice parameters, calculated electronic structures show that $PbH_4(H_2)_2$ is metallic at 200 GPa. For $SiH_4(H_2)_2$ and $GeH_4(H_2)_2$ reported previously, they remain the characteristics of insulator under low pressure. The insulator-to-metal transition occurs at 92 GPa in $SiH_4(H_2)_2$ and at 48 GPa in $GeH_4(H_2)_2$, respectively. However, we didn't find the transition point of $PbH_4(H_2)_2$. It seems to be metal even in ambient pressure, which consist with PbH_4^{31} . So the low pressure metallization does not come from the intercalation of H₂ molecules. Comparing with Si and Ge, Pb has larger ionic radius which results in more strong itinerant property of valent electrons. Figure 4 shows the projected density of state (PDOS) at several selected pressures. According to the electronic PDOS at Fermi level we can draw a conclusion that at low pressure in *Pnnm* structure the Pb-*p* electrons make the most contribution to density of state and exhibit properties of a nearly free-electron metal (Fig. 4a,b). As the pressure increases, the strengthening of H_2 - H_2 interaction leads to the overlap of H-s wave functions. The contribution of H-s electrons to Fermi surface increases. PDOS tends to be uniform distribution, and the bandwidth further broadens from 100 GPa to 300 GPa (Fig. 4c-f). It indicates that with the increase of pressure $PbH_4(H_2)_2$ mainly like to be Pb- H_2 alloy. The Pb interlayer interaction is connected by these H_2 molecules. To gain more insight into the bonding nature of $PbH_4(H_2)_2$, the electron location function (ELF) of C2/m phase at 200 GPa was calculated. ELF shown in Fig. 5 displays the electronic location around Pb and H atoms as well as the nearly free-electron-like distribution among Pb atoms. However, the high ELF values between Pb and H atoms (Fig. 5a) and of intermolecular H_2 (Fig. 5b) indicate that the electrons become delocalized, suggesting a feature of nearly free-electron metal.

The phonon dispersion curves for C2/m structure at 200 GPa (Fig. 6) and other selected pressure point (see Supplementary Fig. S2 online) were calculated to explore the lattice dynamics of PbH₄(H₂)₂. The absence of any imaginary frequencies implies the dynamical stability of C2/m phase under high pressure. The whole phonon spectrum can be divided into three parts. By combining with the phonon density of states (PhDOS) projected on atoms shown in Fig. 7a, in the case of 200 GPa, we find that the low-frequency vibration below 215 cm^{-1} mainly come from the vibrations Pb atoms. The intermolecular strong phonon coupling among H₂ molecules appear in the intermediate-frequency range of 295–1876 cm⁻¹. After a large gap, in high frequency area above $2695-2898 \text{ cm}^{-1}$, the H-H vibration in H₂ formed by H3 and H4 sites mainly contributes in the range of $2695-2898 \text{ cm}^{-1}$, while the vibration in H₂ formed by H1 and H2 sites around 3220 to 3380 cm^{-1} . Comparing these three systems of Si-, Ge-, and Pb-based, we find a strong phonon coupling between silicon and hydrogen in SiH₄(H₂)₂²³, very weak phonon coupling between metal and hydrogen in GeH₄(H₂)₂²⁵ as well as PbH₄(H₂)₂. The H-H vibration in H₂ molecule is the strongest in PbH₄(H₂)₂. From the Eliashberg phonon spectral function $\alpha^2 F(\omega)$ and the integrated EPC parameter $\lambda(\omega)$ shown in Fig. 7b, the intermediate-frequency (295–1876 cm⁻¹) vibrational modes of H₂ molecules contribute 81.5% of total λ . This percentage is larger than 66% in



Figure 4. Electronic PDOS at different pressures. Calculated PDOS of $PbH_4(H_2)_2$ at different pressures of 5 GPa (**a**) and 20 GPa (**b**) for *P*-1 phase, 100 GPa for *Pnnm* phase (**c**), 160 GPa (**d**), 200 GPa (**e**), and 300 GPa (**f**) for *C*2/*m* phase. The lines at zero indicate the Fermi level.





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Figure 6. Phonon spectrum. Calculated phonon spectrum of C2/m structure at 200 GPa.



Figure 7. Phonon properties and Eliashberg spectral function. Calculated phonon density of states (PhDOS) (**a**), and the Eliashberg phonon spectral function $\alpha^2 F(\omega)$ and electron-phonon integral $\lambda(\omega)$ (**b**) for the *C*2/*m* structure at 200 GPa.

Si-based and 75% in Ge-based case. This result highlights the significant role played by H_2 molecules on the electron-phonon interaction.

At 200 GPa, the calculated total EPC constant λ is 1.296 for C2/m PbH₄(H₂)₂. From Si to Ge and then to Pb case, the λ gradually decreases from 1.625 to 1.43 and then to 1.296, which implies a weak coupling between metal and hydrogen. However, the phonon frequency logarithmic average ω_{log} rises gradually, from 871 K in SiH₄(H₂)₂ to 1051 K in PbH₄(H₂)₂. This means more higher Debye temperature in PbH₄(H₂)₂. Based on the obtained $\alpha^2 F(\omega)$ and $\lambda(\omega)$, we now can analyze the superconductivity using the modified McMillan equation by Allen and Dynes³⁶,

$$T_c = \frac{\omega_{log}}{1.2} exp\left(-\frac{1.04(1+\lambda)}{\lambda - \mu^*(1+0.62\lambda)}\right). \tag{1}$$

With the typical choice of the Coulomb pseudopotential $\mu^* = 0.1^3$, a remarkable large T_c of 103 K was obtained for C2/m phase of PbH₄(H₂)₂, which is comparable with those of copper oxide superconductors.

To figure out the pressure effect on superconductivity in PbH₄(H₂)₂, in addition, the T_c values at several typical pressure points were calculated and shown in Supplementary Fig. S3 online. An interesting phenomenon exhibits the superconductivity firstly strengthening before weakening. The T_c has a maximum between 140 and 350 GPa, ~107 K for $\mu^* = 0.1$. Seen from the distances of among H₂ molecules shown in Fig. 3b, the monotonously decreasing makes a hint of "hardening" of intermediate-frequency phonon with the increase of pressure. The phonon spectra shown in Supplementary Fig. S2 online confirm this point. To analyze this phenomenon of T_c variations, we have further calculated the Eliashberg phonon spectral function and the EPC strength at different pressures, the results are presented in Supplementary Fig. S4 online. With the increase of pressure, the calculated EPCs are 1.280, 1.296, 1.379, and 1.341 for 180 GPa, 200 GPa, 250 GPa, and 300 GPa, respectively, which shows a tendency of first increase and then decrease similar to T_c . In the T_c rising zone, the contribution of Pb-H coupling to the EPC strength is decreased from 14.3% at 180 GPa to 12% at 200 GPa, and the phonon vibration of H-H

in H₂ units also weakens the EPC (The contribution is from 7.3% to 6.5% corresponding pressures.). However, the contribution of H₂-H₂ coupling to the EPC is strengthening from 78.4% at 180 GPa to 81.5% at 200 GPa. So the initial rising of T_c results from the contribution increasing of H₂-H₂ for the EPC. As shown in Fig. S4 online, from 75.8% at 250 GPa to 73.5% at 300 GPa, the decrease of contribution of H₂-H₂ for the EPC leads to the fall of T_c . The result further reveals the significance of H₂-H₂ coupling to superconductivity in PbH₄(H₂)₂.

Discussion

Thus far, the stability of $PbH_4(H_2)_2$ has been identified in the pressure range of 0-400 GPa. At low pressure it is metastable and possibly decomposes into $Pb + H_2$ or $PbH_4 + H_2$. Above 133 GPa, it is stable not only thermodynamically but also dynamically. This high-pressure stable phase of C2/m exhibits the expected superconductivity of $T_c \sim 107 \,\mathrm{K}$ at 230 GPa, which is obviously higher than those of conventional group-IV hydrides such as silane, germane, and stannane. Noticeably, the coupling between group-IV element and hydrogen reduces with the increase of atomic number. Namely, the contribution of group-IV element to total EPC decreases in hydrides from 33% in $SiH_4(H_2)_2^{23}$ to 25% in $GeH_4(H_2)_2^{25}$ and then to 12% in $PbH_4(H_2)_2$. On the contrary, the coupling among H_2 molecules strengthens as mentioned above. Particularly, we want to point out that the T_c (~100 K) is comparable for SiH₄(H₂)₂, $GeH_4(H_2)_2$, and $PbH_4(H_2)_2$ at the same Coulomb pseudopotential, though the superconducting mechanism is incompletely same. The intercalating H_2 molecules into group-IV hydrides really improves the T_c . From the phonon contribution to EPC, we find that the intermediate-frequency phonon is dominated. Comparing with corresponding SiH_4^8 , GeH_4^{11} , and SnH_4^{12} , it is clear that the intercalation of H_2 molecules results in the softening of intermediate-frequency phonon. As increasing the content of hydrogen in group-IV elements, it results in enhancing the EPC strength that is dominated by the coupling of the H_2 molecular in the $AH_4(H_2)_2$ (A = Si, Ge, Sn, and Pb) crystals. This is just the origin of higher T_c in H₂-containing compounds. Furthermore, we infer that the higher T_c may be obtained if more H₂ are inserted in group-IV hydrides. Actually, more future works are needed to advance the T_c and understand the superconductivity.

As a comparison, the high-pressure structure of PbH₄(H₂)₂ is visibly different from other hydrogen-rich compounds with high T_c , such as CaH₆³⁷ and (H₂S)₂H₂³². In high-pressure structures of CaH₆ and (H₂S)₂H₂, the H₂ quasi-molecules have been broken, with the strong bonds forming between metal and hydrogen atoms. Although the EPC is mainly contributed by hydrogen, the superconducting mechanism is different. It is the H-H coupling in CaH₆ and (H₂S)₂H₂, while the H₂-H₂ coupling in PbH₄(H₂)₂. It is interested that the H₂ quasi-molecule form keeps all along at thus high pressure up to 400 GPa. At the same time, Pb is one of the heaviest elements. The combination with the lightest H is one of the most important physical problems in high-pressure research. Pb metal makes the metallization pressure of hydrogen-rich compound decrease. Remarkably, the decomposition pressure point (133 GPa) of PbH₄(H₂)₂ is the lowest among these H₂-containing compounds of Si-, Ge-, and Pb-based. This value is much lower than the metallization pressure of bulk molecular hydrogen, which indicates the feasibility to experimentally observe. Hence, Pb-based hydrides are the potential candidates as high- T_c superconductors research in H₂-containing hydrides.

Methods

The search for crystalline structures of $PbH_4(H_2)_2$ phases was performed using particle swarm optimization methodology as implemented in the CALYPSO program^{38,39}. Structural optimizations, enthalpies, and electronic structures were calculated using the Vienna ab initio simulation (VASP) program^{40,41} and projector-augmented plane wave (PAW) potentials employing the Perdew-Burke-Ernzerhof (PBE) functional⁴². The 1s¹ and 6s²6p² electrons were included in the valence space for H and Pb atoms, respectively. For the plane-wave basis-set expansion, an energy cutoff of 800 eV was used. Dense *k*-point meshes were employed to sample the first Brillouin zone (BZ) and ensured that energies converged to within 1 meV/atom. All forces acting on atoms were converged 0.001 eV/Å or less, and the total stress tensor was reduced to the order of 0.01 GPa. With the noteworthy mass ratio 207:1 between Pb and H, we have involved the spin-orbit effect in this calculation.

Based on the optimized structures from VASP, lattice dynamics and superconducting properties were calculated using density functional perturbation theory⁴³ and the Troullier-Martins norm-conserving potentials⁴⁴, as implemented in the QUANTUMESPRESSO code⁴⁵. The cutoff energies of 60 and 400 Ry were used for wave functions and charge densities, respectively. $12 \times 12 \times 8$ Monkhorst-Pack *k*-point grid with Gaussian smearing of 0.03 Ry was used for the phonon calculations at $3 \times 3 \times 2$ *q*-point mesh, and double *k*-point grid was used in the calculation of the electron-phonon interaction matrix element.

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Author Contributions

G.H.Z. and C.L.Y. designed research. Y.C., C.Z. and T.T.W. performed research. Y.C., C.Z., T.T.W., C.L.Y., G.H.Z., X.J.C. and H.Q.L. analyzed the results. Y.C., C.L.Y. and G.H.Z. wrote the first draft of the paper and all authors contributed to revisions. All authors reviewed the manuscript.

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